## Corrections and additions to:

Matrix Algebra<br>Econometric Exercises 1 Cambridge University Press, 2005

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Below we have compiled a list of typos, errors, ambiguities, and additions, both as a service to our readers and as a reminder to ourselves to be included in possible reprints of the book.

Some of the items are very trivial, but still need to be attended to; others involve typos and errors.

We are always on the look-out for mistakes and we encourage our readers to report them to us. Please address your comments to Jan Magnus at magnus@uvt.nl.

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## Exercise 3.53 (page 69)

From line 4 to line 12, each occurrence of $\boldsymbol{x}$ (but not of $\boldsymbol{x}_{n}$ and $\boldsymbol{x}_{m}$ ) should be replaced by $\boldsymbol{y}$.

## Exercise 4.27 (page 86)

The solution to (a) should read:
(a) The matrix $|\boldsymbol{A}|$ is nonsingular because $\operatorname{rk}(\boldsymbol{A})=\operatorname{rk}\left(\boldsymbol{A}^{\prime} \boldsymbol{A}\right)=\operatorname{rk}\left(\boldsymbol{I}_{n}\right)=n$.

## Exercise 5.40 (page 118)

In the displayed formula in the exercise, $|A|$ should be boldface: $|\boldsymbol{A}|$.

## Exercise 6.19 (page 141)

Line 4 in the solution runs over the margin.

## Exercise 7.25 (page 167)

In the first line of the solution to (c), replace 'latter' by 'former'.

## Exercise 7.78 (page 198)

In the first display of the solution to (d), the second matrix should be preceded by $\boldsymbol{A}_{(4)}:=$.

## Exercise 7.79 (page 199)

In the second line from the bottom, Exercise 7.78 is employed (not 7.77 as written).

## Exercise 7.91 (page 206)

Line 2 in the exercise: delete comma after displayed matrix $\boldsymbol{A}$.

## Exercise 8.10 (page 215)

Line 1 in the solution runs over the margin.

## Exercise 8.23 (page 220)

The solution is not as tight as it should be. The correct solution reads as follows.

## Solution

Since $\boldsymbol{A}$ is positive definite, Exercise 8.22 implies that $\boldsymbol{A}=\boldsymbol{B} \boldsymbol{B}^{\prime}$ where $\boldsymbol{B}$ is square. Since $\boldsymbol{A}$ has full rank, so has $\boldsymbol{B}$ (Exercise 4.13(d)). By the QR decomposition (Exercise 7.35), we can write $\boldsymbol{B}^{\prime}=\boldsymbol{Q} \boldsymbol{L}^{\prime}$, where $\boldsymbol{Q}$ is orthogonal and $\boldsymbol{L}$ is lower triangular with positive diagonal elements. Hence, $\boldsymbol{A}=\boldsymbol{B} \boldsymbol{B}^{\prime}=$ $L Q^{\prime} \boldsymbol{Q} L^{\prime}=\boldsymbol{L} \boldsymbol{L}^{\prime}$.

## Exercise 8.69 (page 239)

The last two lines of the solution should be replaced by:
Now premultiply both sides by $\boldsymbol{V}^{-1 / 2}$ and postmultiply both sides by $\left(\boldsymbol{X}^{\prime} \boldsymbol{X}\right)^{-1}$. Upon transposing, we obtain the required equality. (Compare Exercise 12.29.)

## Chapter 9, Introduction (page 245)

Last line: "theeigenvalues" should be "the eigenvalues".

## Exercise 9.11 (page 253)

Line 1 should read: "Let $\boldsymbol{C}$ and $\boldsymbol{D}$ be two real $n \times n$ matrices, $\ldots$ "
The reason for restricting $\boldsymbol{C}$ and $\boldsymbol{D}$ to be real (which is only needed for part (a)) is that the logarithmic function is multiple-valued, even in the case of a scalar complex variable. Taking logarithms on both sides of an equation, the equality may not hold anymore if the principal value is taken on both sides.

## Exercise 12.1 (pages 322-323)

In the solution to $b$ ), second line: $\left(1 / \boldsymbol{b} \boldsymbol{b}^{\prime}\right) \boldsymbol{b} \boldsymbol{b}^{\prime}$ should read $\left(1 / \boldsymbol{b}^{\prime} \boldsymbol{b}\right) \boldsymbol{b} \boldsymbol{b}^{\prime}$. Also, in the solution to $c$ ), third line from the end: "if and only" should read "if and only if".

## Exercise 13.25 (page 366)

Line 5 from bottom: At the end of the formula giving $\mathrm{D} \boldsymbol{F}(\boldsymbol{X})$, the differential dvec $\boldsymbol{X}$ should be removed.

## Exercise 13.38 (page 373)

Last line: "dvec $(\boldsymbol{Y})=\boldsymbol{D}^{+}$dvec $\boldsymbol{Y}=\ldots$ " should be:
$" d \operatorname{vech}(\boldsymbol{Y})=\boldsymbol{D}^{+}$dvec $\boldsymbol{Y}=\ldots$..

## Exercise 13.53 (page 382)

Line 9: displayed formula should end with full stop (.).

## Exercise 13.56 (page 384)

Line 1: "Then, since $\boldsymbol{R}^{\prime} \boldsymbol{\beta}=\boldsymbol{c}$, we find the solution for $\boldsymbol{l}$ as" should be: "Then, denoting the constrained solution by $(\tilde{\boldsymbol{\beta}}, \tilde{\boldsymbol{l}})$, we have $\boldsymbol{R}^{\prime} \tilde{\boldsymbol{\beta}}=\boldsymbol{c}$, and hence"

Line 4: $\boldsymbol{X} \boldsymbol{\Omega}^{-1} \boldsymbol{X}$ should be $\boldsymbol{X}^{\prime} \boldsymbol{\Omega}^{-1} \boldsymbol{X}$.

## Appendix A, Section A.3.4 (page 408)

Line 17: the formula

$$
f^{(n)}(c)(x-c)^{n} / n!
$$

should read

$$
f^{(n)}(c)(x-b)^{n} / n!
$$

